

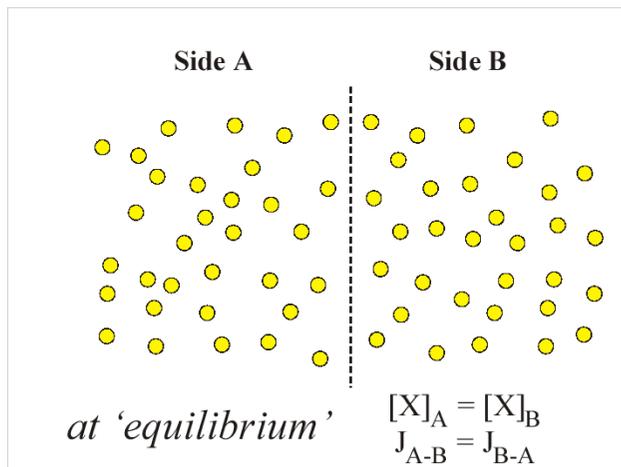
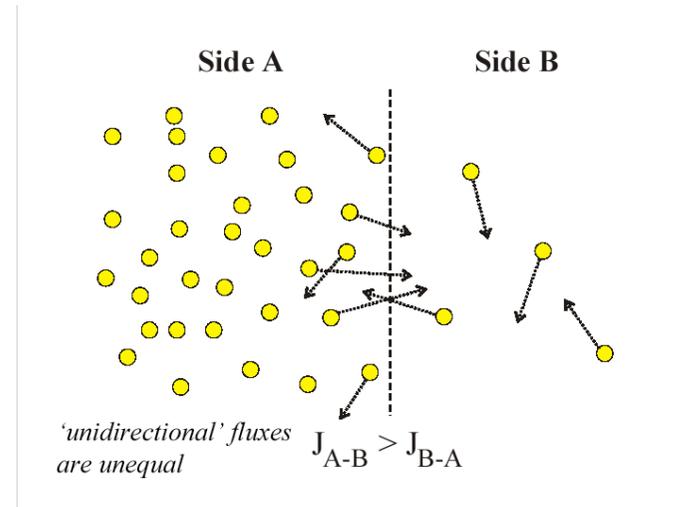
DIFFUSION



Molecular diffusion, often simply called diffusion, is the **thermal motion** of all particles at temperatures above absolute zero

A single molecule moves around randomly.

With more molecules, there is a clear trend where the solute fills the container more and more uniformly.



With an enormous number of solute molecules, all randomness is gone: The solute appears to move smoothly and systematically from high-concentration areas to low-concentration areas, following Fick's laws.

flux

$$J = \frac{dn}{dt} \frac{1}{A}$$

n=number of particles

t=time

A=area

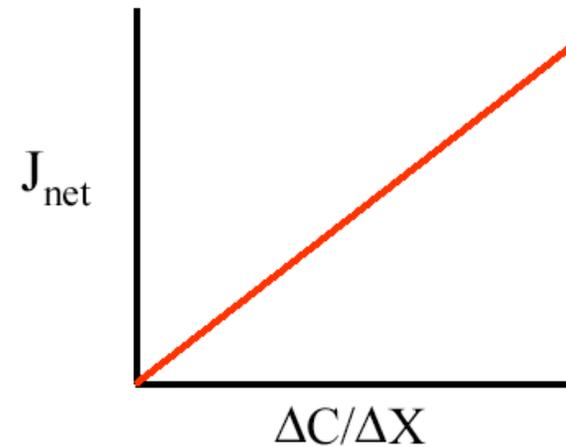
$$J = -D \frac{dc}{dx}$$

I FICK'S LAW

Free diffusion of
uncharged particles in
1 spatial dimension

Fick's law in finite form :

$$J = -D \frac{\Delta c}{\Delta x}$$



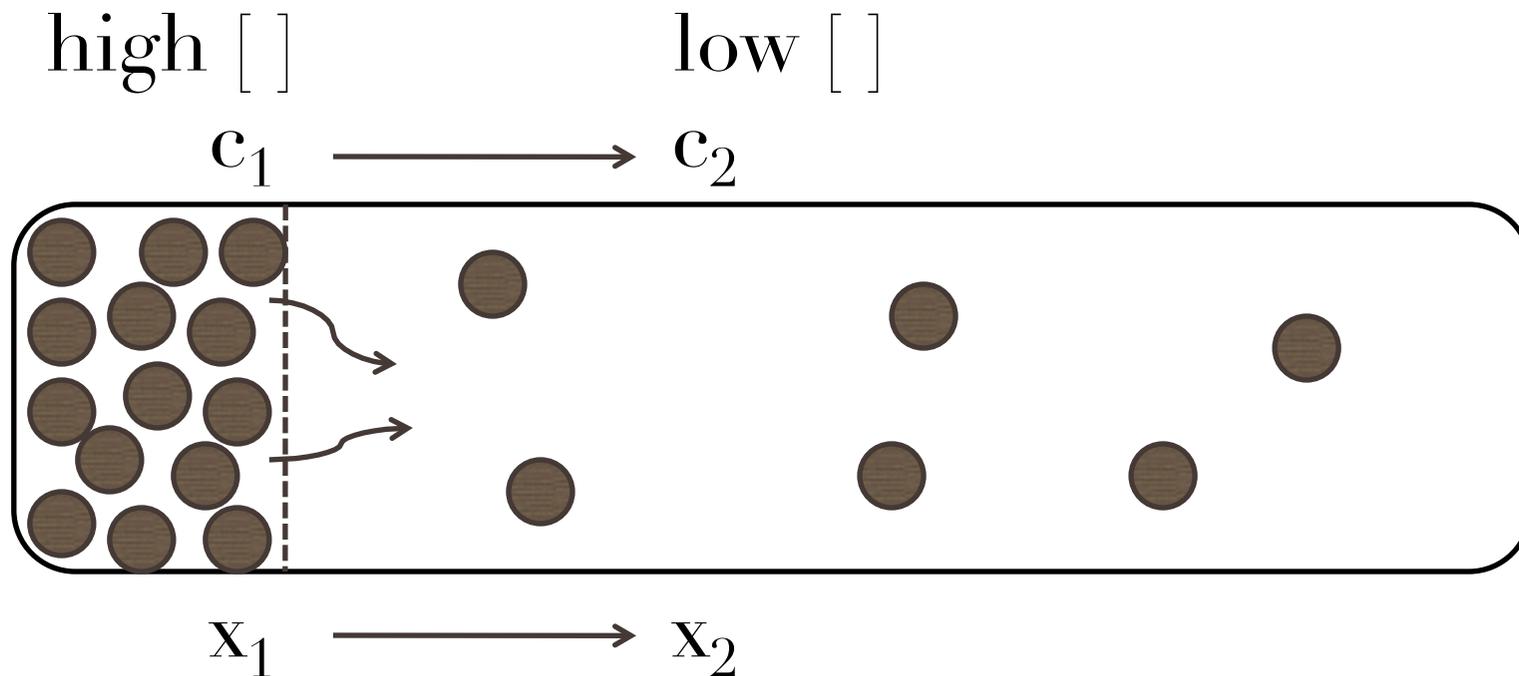
$$J = -D \frac{\Delta c}{\Delta x}$$

since

$$\Delta c < 0 \quad (c_2 < c_1)$$

$$\Delta x > 0 \quad (x_2 > x_1)$$

to have a positive flux



diffusion constant $D = \frac{RT}{Nf}$

for a solid macroscopic body STOKES law can be applied:

$$v = \frac{F}{f} \quad (\text{STOKES})$$

$F = \text{force}$ (on a single particle) $v = \text{velocity}$ $f = \text{frictional resistance}$

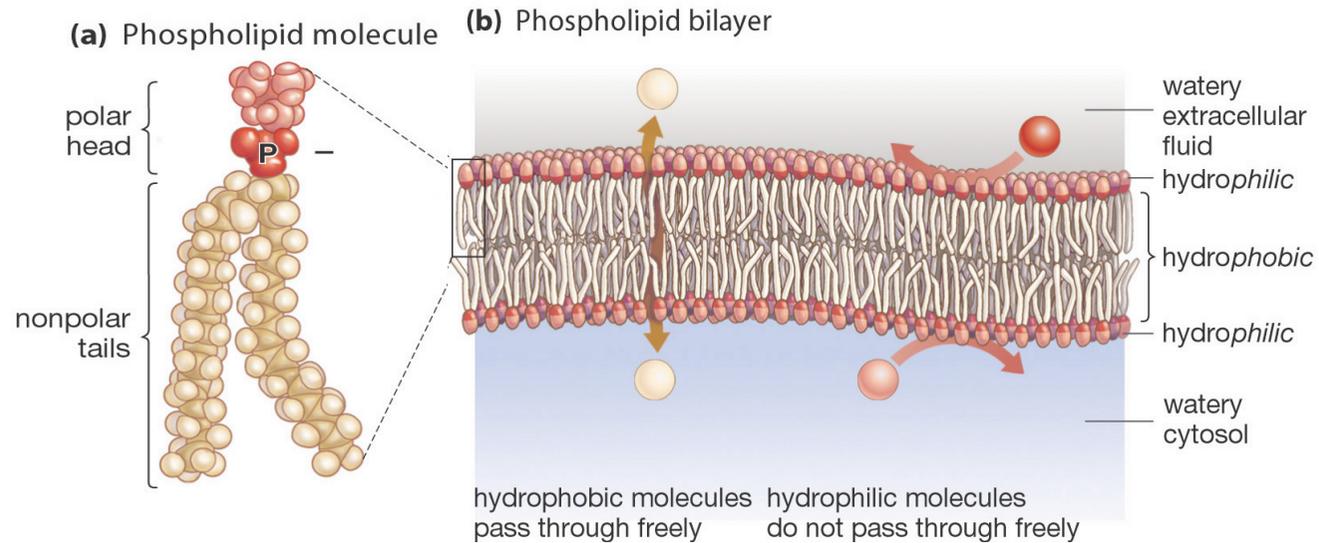
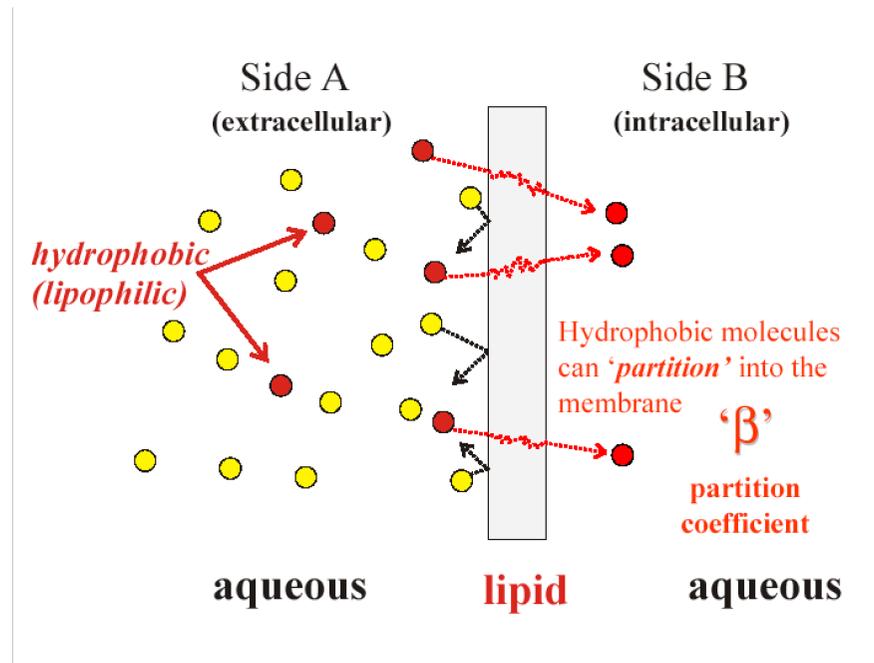
$f = 6\pi\eta r$ $\eta = \text{solvent viscosity}$ $r = \text{particle radius}$

$$D = \text{velocity} = \frac{A}{t} = \frac{\mu m^2}{s}$$

$$J = \frac{\frac{\mu m^2}{s} \cdot \frac{mol}{\mu m^3} \cdot \frac{1}{\mu m}}{\frac{1}{\Delta x}} = \frac{mol}{\mu m^2 s}$$

D Δc $\frac{1}{\Delta x}$

Diffusion through a biological membrane



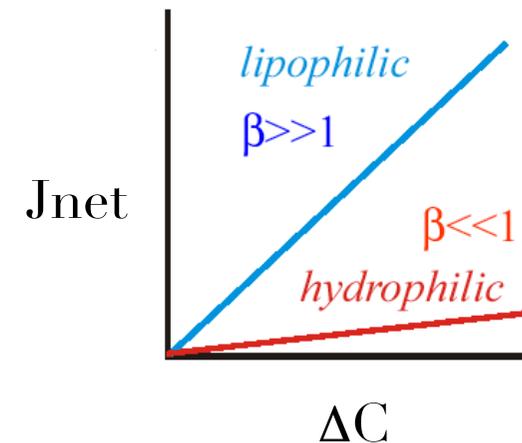
In the case of a diffusional flux through a real biological membrane FICK's law can be written as

$$J = D\beta \frac{\Delta c}{\Delta x}$$

in which $\beta =$ partition coefficient $= \frac{c_m}{c}$

gives the actual concentration of the particle in the membrane

Δx is now the membrane thickness

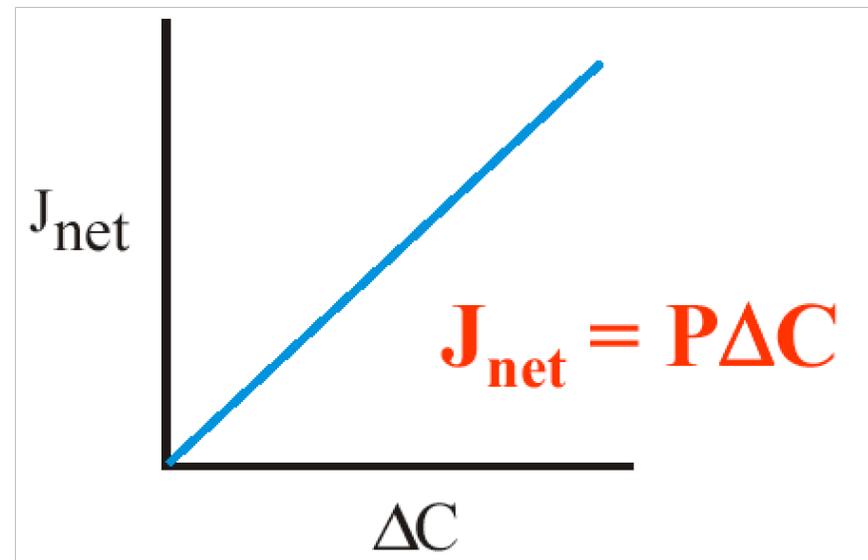


$$J = D\beta \frac{\Delta c}{\Delta x}$$

if we call PERMEABILITY $P = \frac{D\beta}{\Delta x}$

FICK'S equation finally becomes very simple!

$$J = P_m \Delta c$$



FICK's laws apply to un-charged particles.

WHAT ABOUT ION FLUXES?

the driving force is the ELECTROCHEMICAL POTENTIAL
(CHEMICAL + ELECTRICAL POTENTIAL)

$$\mu_c = RT \ln c$$

$$\mu_e = zF\varphi$$

$$\mu_{ec} = \mu_c + \mu_e = RT \ln c + zF\varphi$$

$$J = -D \left(\frac{dc}{dx} + c \frac{zF}{RT} \frac{d\varphi}{dx} \right) \quad \text{NERNST-PLANCK}$$